DEPARTMENT OF MECHANICAL ENGINEERING & MECHANICS COLLEGE OF ENGINEERING & TECHNOLOGY OLD DOMINION UNIVERSITY NORFOLK, VIRGINIA 23529

### ITERATIVE METHODS FOR LARGE SCALE STATIC ANALYSIS OF STRUCTURES ON A SCALABLE MULTIPROCESSOR SUPERCOMPUTER

LANGLEY

GRANT

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By

Nahil A. Sobh, Principal Investigator

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#### Final Report

## ITERATIVE METHODS FOR LARGE SCALE STATIC ANALYSIS OF STRUCTURES ON A SCALABLE MULTIPROCESSOR SUPERCOMPUTER

#### NAHIL ATEF SOBH<sup>1</sup>

A parallel Preconditioned Conjugate Gradient (PCG) iterative solver has been developed and implemented on the iPSC-860 scalable hypercube. This new implementation makes use of the PARTI (Parallel Automated Runtime Toolkit at ICASE) primitives to efficiently program irregular communications patterns that exist in general sparse matrices and in particular in the finite element sparse stiffness matrices.

The iterative PCG has been used to solve the finite element equations that result from discretizing large scale aerospace structures. In particular, the static response of the High Speed Civil Transport (HSCT) finite element model cited in reference [3] is solved on the iPSC-860.

The preconditioned conjugate gradient algorithm implemented on the iPSC is outline below.

We have parallelizied the following three crucial steps:

- 1. The matrix vector multiplication (Kp).
- 2. The inner products  $(z^T r \text{ and } p^T (Kp))$ .
- 3. The solution of the preconditioning step (Mz = r).

Principal Investigator, Assistant Professor Department of Mechanical Engineering and Mechanics

1. $u_0$		(Initialize displacements)
$2. r_0 = f - Ku$		(Initialize residual 'out of balance forces')
3. for $k = 1, 2,$ do		(Iteration loop on $k$ )
4. if $  r_{k-1}   \leq \text{tolerance}$ ,	exit	(If equilibrium is satisfied 'exit')
$Solve  Mz_{k-1} = r_{k-1}$		(Solve for the iteration vector)
6. $\beta_k = \frac{z_{k-1}^T r_{k-1}}{z_{k-2}^T r_{k-2}}$	$(\beta_1=0)$	(Evaluate the scaling parameter)
7. $p_k = z_{k-1} + \beta_k p_{k-1}$	$(p_1=z_0)$	(Update search direction)
8. $\alpha_k = \frac{z_{k-1}^T r_{k-1}}{p_k^T K p_k}$		(Evaluate new step length)
$9.   u_k = u_{k-1} + \alpha_k p_k$		(Update displacements)
$10.   r_k = r_{k-1} - \alpha_k K p_k$		(Update residuals 'out of balance forces')
11. end of for loop		(go to 3)

Good preconditioners are those which approximate or mimic the operational role of the original problem. Thus the preconditioning step given in the PCG algorithm involves solving a system, Mz = r, which is very close to the original system, Ku = f. The communications overhead constraint imposed by MIMD machines limit the use of highly coupled direct solvers. Therefore we have used an approximation to K that has a loosely coupled structure. In particular, we have used a diagonal, i.e., point Jacobi preconditioner. Jacobi type preconditioners parallelize very well on MIMD and SIMD supercomputer architectures. Although they may look simple it has been shown that their overall performance can be very competitive when compared to other preconditioners. We have also implemented a block SSOR family of preconditioners. The SSOR family of preconditioners accelerate the convergence rate but at the expense of extra computations and less communications. The current work is focusing on the trade off between communications and computations when using the SSOR preconditioners.

Computer listing of the C program is given in the appendix.

This research has accomplished the following tasks:

- 1. Implemented a conjugate gradient iterative solver for symmetric and sparse matrices on the Intel iPSC-860 hypercube at ICASE.
- 2. Implemented SSOR and point -Jacobi preconditioners to accelerate convergence of the conjugate gradient iterative solver and reduce communications.
- Generated large-scale finite element models of structures using the COMET software at NASA Langley Research Center. Performed linear static analysis on the generated structural models on the Intel iPSC-860 at ICASE/NASA-Langley.
- 4. A general purpose software has been implemented to generate full stiffness matrices given the symmetric part from COMET.

No. of	CPU time (seconds)	CPU time (seconds)	
Processors	diagonal preconditioning	SSOR	
High Speed Civil Transport (HSCT) (16,146 equations)			
8	1342		
16	786	764	
32	565	438	
Blade Siffened Panel (BSP) (1,824 equations, )			
1	2.5	3.0	
2	2.1	2.1	
4	1.8	1.4	
8	1.9	1.3	
16	1.7	1.2	

The table shown above summarizes the performance of the preconditioned conjugate gradient iterative solver. The first column is the number of processors used to solve the above mentioned problem, the second column corresponds to the amount of cpu time in seconds required to solve a given problem using the diagonal of the stiffness matrix as a preconditioner. The third column is the cpu time in seconds required to solve a given problem using a symmetric successive over relaxation preconditioner.

The speedup performance on the large problem (HSCT) is modest. The speedup performance is expected to be better as the number of equations is increased. Although one may think that a direct solver will be much more efficient on these problems, one should not ignore the fact that direct solvers require extensive amount of storage which limit the amount of equations one can solve. Thus *iterative solvers will find most of their efficient use on super large problems* which exceed in their size the core memory available on a given supercomputer. This limitation should drive one to use out-of-core solvers which are slow compared to iterative solvers and are not easy to parallelize. Therefore efforts should concentrate on developing efficient parallel out-of-core solvers and iterative solvers with emphasis on parallelizable preconditioners to efficiently use the future technology of massively parallel supercomputers.

#### References

- Berryman, H. and Saltz, J. A Manual for PARTI Runtime Primitives, ICASE Interm Report 13, September 1990.
- 2. Golub, G. H. and Van Loan, C. F., *Matrix Computations*, The John Hopkins University Press, 1983.
- 3. Poole, E. L., Knight, N. F. and Davis, D. D., High-Performance Equation Solvers and Their Impact on Finite Element Analysis, Finite Element Methods in the Design Process, ed. by Robinson, J., England, 1990

#### Appendix

#### Computer Listing

elp1.c

```
char *argv[];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      main (argc, argv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          #define BUFFER_SIZE 1000
#define ROW_COEF_MSG 111
#define ROW_INDX_MSG 222
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int argc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         define MAX_NUM_PROC 32
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           define SETUP_MSG 22323
        •
             /* Check if input files are available then open them.
                                                                                                                                                                                  FILE *fp,
                                                                                                                                                                                                                                                                                                                        float coef_buffer(MAX_NUM_PROC)[BUFFER_SIZE], /* Stifness coefficients
    /* in lower triangluar */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int rows_per_proc, /* No. or rows a
setup_buffer[1 + MAX_NUM_PROC];/*
                                                                                                                                                                                                                                                                                                                                                                                                                    int remainder,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int negns,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int nmyrows [MAX_NUM_PROC],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 1nt 1,
                                                                                                                                                                                                                                      float tol; /*CG param. */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       numjnt,
dof,
jdof,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        lth,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             junk,
1k11,
                                                                                                                                                                                                                                                                                                                                                                                                 curr_max;
                                                                                                                                                                                                                                                                                                                                                                                                                                                        nproc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ptr,
                                                                                                           *dlag,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      proc,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nrows,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      nmysends [MAX_NUM_PROC],
                                                                                           forc,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ncols;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            nonzeros,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        indx_buffer[MAX_NUM_PROC]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  buffer_size(MAX_NUM_PROC), /* Array of buffers sizes for sending data. */
    /* Max MAX_NUM_PROC, reflects the number of */
                                                                                                                              *coefs,
                                                                                                                                                *indxs,
                                                                                                                                                                  pt rs,
                                                                                                                                                                                                                     max_itr; /*CG param.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [BUFFER_SIZE]; /* Array of buffers for row-location coefficients */
/* distributed over available processors (max=MAX_NUM_PROC) */
                                                                     /* Generic file pointer */
, /* Index location file */
s, /* Stiffness coefficients file */
, /* Diagonal stiffness file */
, /* Nodal Forces file */
Problem Statement file */
                                                                    /* Nodal Forces file
/* Problem Statement file
                                                                                                                                                                                 /* Generic file pointer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            /* No. of rows assigned to a processor */
                                                                                                                                                                                                                                                                                                                                                                                                                                                   /* Number of processors allocated
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ;;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         /* Number of nodes
/* Degrees of free
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               /* Number of equations
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   /* Number of columns
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     /* A processor counter
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     /* An integer pointer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     /* No. of rows
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  /* processors available (update to 1024,..) */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         /* Dummy integer counter
/* Dummy integer counter
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 /* I.D. for
/* Maximum number of processors
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   /* Length of the buffer array
/* I.D. for stiffness coefficients
/* I.D. for row-location coefficients
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Row-length for sparse matrix storage
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Total number of unconstraint equations */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Degrees of freedom per node
                                                                                                                                                                                                                     *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /* Integer number of rows per processor */
/*
                                                                                                                                                                                                                                                                /* Pointer to a floating
/* point number.
                                                                                                                                                                                                                                                                                                         /* form.
:::
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      22222
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 !!!!!
                                                                                                                                                                                                                                                                                                                                                                                                 !!
                                                                                                                                                                                                                                                                                                                                           *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           *
```

```
If ( d1ag=fopen("K.DIAG","r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                     if( ( coefs=fopen("K11.COEFS","r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if( [ indxs=fopen("K11.INDXS","r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  . .
                                                                                                                                                                                             * Diagonal stiffness coefficients.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if( ( ptrs=fopen("K.PTRS", "r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              1f( ( info=fopen("K.INFO", "r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                * Stricly lower triagular stiffness matrix coefficients.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              * Columns locations for sparse matrix data-structure.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                * Problem definition.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     -----
fprintf(stderr, "Error: cannot open %s for input\n", "K.DIAG");
                                                                                                                                                                                                                                                                                                                                                              exit (1);
                                                                                                                                                                                                                                                                                                                                                                                fprintf(stderr, "Error: cannot open %s for input\n", "Kil.COEFS");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ex1t(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   fprintf(stderr, "Error: cannot open %s for input\n", "K11.INDXS");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ex1t(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fprintf(stderr, "Error: cannot open %s for input\n", "K.PTRS");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           exit(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fprintf(stderr,"Error: cannot open %s for input\n","K.INFO");
```

Applied nodal forces

```
fprintf(stderr,"Error: cannot open %s for input\n","K.FORC");
                                                                                                                                                                                                                                                                                                                                                                                                                                                 * Load all "-1" nodes with program "unst4" with process id "0".
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               total number of degrees of freedom before constraints
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   * Diagnostic message to compare
* total number allocated nodes with those defined by the user.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * negns - number of equations in non-singular input matrix
()dof - number of constrained dofs)
* lkii - number of non-zero coefficients below main diagonal

    Initialize buffers equal the number of allocated nodes.

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         printf("begin host: number of processors is td\n", nproc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          * Initialize number of messages sent to a given node.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /* read info file containing problem size parameters

* numjnt - number of joints in FEM model

* dof - degrees of freedom per joint
                                                                                                                                                                                                                                   process 1d=1 for host program.
1f( ( forc=fopen("K.FORC","r") ) == NULL )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             * Get the number of total allocated nodes.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (num]nt X dof)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for ( 1=0; 1<nproc; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   buffer_size[1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               nmysends[1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                load("elp2", -1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              nproc=numnodes();
                                                                                                                                                                                                                        Set NX/RX
                                                                                        ex1t(1);
                                                                                                                                                                                                                                                                                                                                            setp1d(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               * )dof
```

elp1.c

```
fprintf(stderr, "Grrrrrr.....nproc=%d, proc= %d\n", nproc, proc);
                                                                                                                                                      /* compute number of rows per processor for blocked row assignment, * whenever the number of equations is not an even multiple of
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * for each row determine which processor then read in that row
* from data files and place coefficients in the appropriate buffer
                                                                                                                                                                                                             * the number of processors, the remaining rows are distributed in * sequential order to the nodes.
                                                                                                                                                                                                                                                                                                                                                                                  /* Equal Shares of rows */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       curr_max = curr_max + rows_per_proc + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         * if buffer doesn't have enough room, flush it.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      curr_max = curr_max + rows_per_proc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     1f( BUFFER_SIZE<=buffer_size(proc] + lth+2 )</pre>
                                                                             r=%d\n", numjnt, dof, jdof, neqns, lk11, tol, max_itr);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                * get number of nonzeros in current row
                                                                                                                                                                                                                                                                                                                                                                                                                          /* Error in logic here .. feb. 26, 1991 */
/* remainder = nrows % rows_per_proc; */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   printf("remainder = %d \n", remainder);
if( remainder > 0 )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1f( (proc>=nproc) | (proc<0) )</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     /* Remaining shares if not zero */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        curr_max = rows_per_proc - 1;
                                                                                                                                                                                                                                                                                                                                                                        rows per proc = nrows / nproc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1f( remainder>proc+1 )
                                                                                                                                 /* csend(333,tol,4,-1,0);*/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  curr_max = rows_per_proc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                fscanf(ptrs,"td", &lth);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               remainder = nrows % nproc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for( 1=0; 1<nrows; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1f(1 > curr_max)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  proc=proc+1;
                                                                                                                                                                                                                                                                                                                       nrows = negns;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              broc=0;
```

```
printf(" send message: type, proc, length \n %d, %d, %d\n",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           csend( SETUP_MSG,setup_buffer,sizeof(int)*(numnodes()+1),-1,0);
                                                                                                                                                                                                                                                                                                            * Tell each processor how many messages to expect
                                                                                                    csend( ROW_COEF_MSG, coef_buffer[1],
    sizeof(float)*buffer_size[1],1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        * close all the filles openned at the beginning
                                                                                                                                                                                                                                                                                                                                                                                                                                              setup_buffer[1] = nmysends[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      setup_buffer(nproc) = nrows;
                                                                                                                                                                                                                                                                                                                                                                                        for( 1=0; 1<nproc; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                SETUP_MSG, -1, nproc+1);
                                                                                                                                                                                   nmysends[1]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fclose(indxs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fclose (coefs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       waitall(-1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fclose (info);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fclase (ptrs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fclose (diag);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        printf("sending messages:type, proc, length\n %d, %d, %d\n %d, %d, %d\n",
ROW_COEF_MSG, i, buffer_size{1},
ROW_INDX_MSG, i, buffer_size{1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Add current row to buffer for appropriate processor First, add lth (number of coefs in this row) and row number
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               * to index_buffer;
* Second, add the diagonal coefficient for this row to first
                                                                                                               printf(" message: type, proc, length \n td, td, td \n",
                                                                                                                                                                                                     *d \n",

    Finally, add the column index values
    to index_buffer and actual coefficients to coef_buffer.

                                                            printf("sending rows off to processor %d \n", proc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                * location in coef_buffer for this row (1.e. ptr2[0])
                                                                                                                                                                                                                                                                                                                                                                                                    s1zeof(float)*buffer_s1ze[proc], proc,0);
                                                                                                                                                                                            printf(" message: type, proc, length \n td, td,
                                                                                                                                                                                                                                                                                                                          stzeof(int)*buffer_stze[proc],proc,0);
                                                                                                                                         ROW_COEF_MSG, proc, buffer_size(proc));
                                                                                                                                                                                                                      ROW_INDX_MSG, proc, buffer_size(proc]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ptr2 = &coef_buffer[proc][buffer_size[proc]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ptr = &indx_buffer(proc)(buffer_size(proc));
                                                                                                                                                                                                                                                                                                csend( ROW_INDX MSG, indx_buffer[proc],
                                                                                                                                                                                                                                                                                                                                                                          csend( ROW COEF MSG, coef_buffer[proc],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     sizeof(int)*buffer_size[1],1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            csend( ROW_INDX_MSG,1ndx_buffer[1],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         /*
* Flush all buffers with something in them
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fscanf(indxs,"%d", &ptr[]+2] );
fscanf(coefs,"%f", &ptr2[]+2]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fscanf(diag,"%f",%ptr2[0]);
fscanf(forc,"%f",%ptr2[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  buffer_size[proc] += 2+lth;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             buffer_size(proc) = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for( j=0; j<1th; j++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1f( buffer_size[1] > 0 ]
                                                                                                                                                                                                                                                                                                                                                                                                                                                            nmysends[proc]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for( 1=0; 1<nproc; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ptr(0) = 1+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ptr[1] = 1th;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       .
                                                                                                                                                                                                                                             •
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          •
```



finclude <stdio.h> !include "part1.h" #include <cube.h> finclude <math.h> finclude "main.h" \* node program. main (argc, argv)

char \*argv(]; int n\_iter; count; int 1,11, int arge;

TTABLE \*table;

SCHED \*sr; float \*z; long start\_time; /\* time in milliseconds \*/
long elapsed\_time;/\* pcg timing in milliseconds \*/

int n\_off\_proc;

Get each node number \*/ • me = mynode();

sprintf(name, "out. %d", me);

myfile=fopen(name, "w");

printf(" begin node program processor %d filename= %s \n",me,name);

fprintf(myfile," begin node program processor %d \n",me);
fflush(myfile);

\* Get sparse matrix from host program.

det\_sparse\_mat();

fprintf(myfile," my nonzeros = td \n",Mynonzeros);
fflush(myfile);

\* Build translation table by scattering Row to the table. \* IN: Row[1]

OUT: table

.

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localize (table, &sr, Cols, LocalCols, Mynonzeros, &n\_off\_proc, Myrows); table = build\_translation\_table(BLOCKED,Row,Myrows);

Solve Kx = f (Iteratively using pcg algor.)

z = (float \*) malloc(sizeof(float)\*Myrows);

z = pcg(sr,n\_off\_proc,Force,0.001,50000,4n\_iter); elapsed\_time = mclock() = start\_time; start\_time = mclock();

fprintf(myfile," elapsed time = td \n number of iterations = td\n", printf(" elapsed time = %d \n number of iterations = %d", elapsed\_time, n\_iter); elapsed\_time, n\_iter);

pr\_float\_array( "z", z, Myrows);

/\* END OF NODE PROGRAM \*/

???? /\* This function is used to read in the sprse mat. /\* It should be ignored if at all possible. /\*

void get\_sparse\_mat() int size,

indx\_buffer[BUFFER SIZE];

float coef\_buffer[BUFFER\_SIZE];

rows\_expected; int type,

rows\_expected = -1; Myrows = 0; Mynonzeros = 0;

gsync();

while( (Myrows<rows\_expected) | (rows\_expected<0) ) cprobe (-1);

size = infocount()/sizeof(int); type = infotype();

crecv( ROW\_INDX\_MSG,indx\_buffer,size\*sizeof(int)); 1f( type==ROW\_INDX\_MSG )

```
fprintf(stderr, "Error on node td : too many rows!!!\n",mynode()];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        fprintf(stderr, Error on node %d : too many nonzeros!!!\n",
crecv( ROW_COEF_MSG, coef_buffer, size*sizeof(float));
unpack_row_data(indx_buffer, coef_buffer, size);
                                                                                                                                    crecv(SETUP_MSG,indx_buffer,size*sizeof(int));
rows_expected = indx_buffer[mynode()];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ncols = Ncols[Myrows] = indx_buffer[count+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                         vold unpack_row_data(indx_buffer,coef_buffer,size)
int *indx_buffer,size;
                                                                                                                                                                                                                                                                                                                                                  ::
                                                                                                                                                                                                                                                                                                                                                                                         /* -----
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Cols(col_count) = indx_buffer(count);
Vals(col_count) = coef_buffer(count);
                                                                                                                                                                                   Nrows = indx buffer[numnodes()];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Row[Myrows] = indx_buffer[count];
Dlags[Myrows] = coef_buffer[count];
Force[Myrows] " coef_buffer[count+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1f ( Mynonzeros >= MAX_NONZEROS )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1f ( Myrows >= MAX_ROWS )
                                                                                       1f ( type==SETUP MSG )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for ( count =0; count < size; )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for( j=0; j<ncols; j++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 static int col_count = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Mynonzeros += ncols;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   mynode());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           count =count +2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               float *coef buffer;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ex1t();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       exit();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               count 2,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int count,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ncols,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      float sum;
                                                                                                                                                                                                                                                     gaync ();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      row,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1st;
                                                                                                                                                                                                                                                                                                                                        १११
```

## elp2-new.c

cal count ++;

count ++;

Myrows++;

```
if( first_row > Myrows )
printf(" me= %d, cannot print rows starting with %d, Myrows=%d\n",
me,first_row,Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  printf(" me= td, cannot print rows past td, Myrows=td\n",
me,last_row.Myrows);
last_row=Myrows;
printf("The value of my nonzeros %d\n", Mynonzeros);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          /* find the starting positions */
printf(" me=td, print_my_rows from td to td\n",
    me,first_row,last_row);
                                                                                                                                                                                        void print_my_rows( first_row, last_row, option )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for ( 1=flrst_row; 1<#last_row; 1++ )</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for ( 1=0; 1<first_row-1; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ptrl = ptrl+Ncols[1];
ptr2 = ptr2+Ncols[1];
ptr3++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              1f( last_row > Myrows )
                                                                                                                                                                                                                                                                                                                                                                                                                                                           1f ( strcmp(option, "all") == 0.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ptr3 = &D1ags[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ptr1 = &Cols(0);
ptr2 = &Vals(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fflush(stdout);
                                                                                                                                                                                                                                                                                                                                            *ptr3;
                                                                                                                                                                                                           int first_row,
                                                                                                                                                                                                                                                                                                                           float *ptr2,
                                                                                                                                                                                                                                 last row;
                                                                                                                                                                                                                                                char *option;
                                                                                                                                                                                                                                                                                      int *ptrl;
                                                                                                                                                                                                                                                                                                                                                                                                                      lth;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else
                                                                                                                                                                                                                                                                                                                                                                                1nt 1,
                                                                                            : :
```

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```
fprintf(myfile," Myrow= %d, Row= %d, Diag Coef= %f, lth= %d\n",
                                                                                                                      fprintf(myfile," column= td, Coef= tf\n", *ptrl, *ptr2);
                                                                                                                                                                                                                                                                         printf(" me= %d, cannot understand print option %s\n",me,option);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fprintf(myfile," Integer Array %s follows: lth=%d\n" ,name,lth);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fprintf(myfile," Float Array %s follows: lth=%d\n" ,name,lth);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [printf(myfile," ts(td)=td\n", name, 1, array[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fprintf(myfile," %s[%d]=%f\n",name,1,array[1]);
                                 1-1, Row[1-1], *ptr3, lth, Ncols[1-1]);
                                                                                                                                                                                                                                                                                                                                                                                                             ;;;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void pr_float_array( name, array, 1th )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void pr_int_array( name, array, ith )
                                                                             for( j=0; j<Ncols[1-1]; j++)

/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for( 1=0; 1<1th; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for( 1=0; 1<1th; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fflush(myf1le);
                                                                                                                                                pt r1++;
                                                                                                                                                                   pt r2++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           fflush(myfile);
                                                        pt x3++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *array;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               char *name;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int *array,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            char *name;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1nt 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1nt 1;
                                                                                                                                                                                                                                                     else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           float
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1.nt
                                                                                                                                                                                                                                                                                                                                                                                                       !!
                                                                                                           column= %d, Coef= %f\n", *ptr1, *ptr2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1-1, Row[1-1], *ptr3,Ncols[1]);
[printf(myfile," Myrow= td, Row= td, Diag Coef= tf, lth= td\n",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fprintf(myfile," column= %d, Coef= %f\n", *ptil, *pti2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              lth=NcoIs(1-1);
print(" Myrow= td, Row= td, Diag Coef= hf, lth= td\n",
                                                                                                                                                                                                                                                                                                                                                                    printf(" me=td, print_my_rows option=limits\n",me);
if (first_row > Myrows)
printf(" me= td, cannot print row td, Myrows= td\n",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1f( last_row > Myrows )
printf(" me= %d, cannot print row %d, Myrows= %d\n",
me,first_row,Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for( 1=0; 1<first_row - 1; 1++ )</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for ( j=0; j<Ncols[1-1]; j++ )
                                                                                                                                                                                                                                                                                                        else if( strcmp(option, "limits") == 0 )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1-1, Row[1-1], *ptr3, lth);
                                                                                                           fprintf(myfile,"
                                                                                                                                fflush (myfile);
                                                              for( j=0; j<lth; j++
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ptrl=ptrl+Ncols[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ptr2=ptr2+Nco1s[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for ( 1=0; i < last_row-1; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                   me, flist_row, Myrows);
                                                                                                                                                                                                                                                                                                                                                 /* find the first row */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ptrl=ptrl+Ncols[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ptr2=ptr2+Ncols[1];
fflush (myfile);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ptr3 = &Diags[0];
                                                                                                                                                        pt r1++;
                                                                                                                                                                           pt r2++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ptr1 = &Cols(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ptr2 = 4Vals(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     /* find the last row */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ptr3 = &Diags[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      pt.13++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1=first row;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pt r1++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pt r2++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ptrl = &Cols[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ptr2 = &Vals{0};
                       pt.r3++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             lth=Ncols[1-1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pt r3++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pt.r3++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1=last row;
                                                                                                                                                                                                                                                                                                                                                                                                                                                            else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                e1 se
```



\* Gather data using previously computed communication schedule. /\* Calculate dot product of distributed vectors x(1),y(1)
/\* Every processor gets copy of the gloabl result
/\* /\* sparse matrix vector multiply function /\* require that the schedule be built and passed in /\* for( j=0; ) fNcols[1]; j++ );
y[1] += x[LocalCols[count]]\*Vals[count];
y[LocalCols[count]] += x[1]\*Vals[count]; \*/ vold spmvm(sr,n\_off\_proc,x,y)
SCHED \*sr; /\* <- communication schedule \*/</pre> \*y; /\* <- input and result vectors \*/ for( 1=0; 1<Myrows+n\_off\_proc; 1++ ) fscatter\_add(sr,&y[Myrows],y); for( 1=0; 1<Myrows; 1++ )+ y[1] += Dlags[1]\*x[1]; fgather(sr,&x(Myrows),x); float result, wrk; int n off proc; float dot(x, y, n) count ++; y[1]=0.0; int count, count = 0; float \*x, float \*x; float \*y; 1nt 1; Int n; •

result = 0;

# elp2-new.c

for (1=0;1<n;1++)

```
SCHED *sr; /* <-communications schedule for sparse matrix-vector multiply */
int n_off_proc; /* number of fetchs (communications) required */
float *rhs; /* <- rhs for rhs=Ax */
float epsilon; /* <- tolerance */
int max_iters; /* <- max # of iterations to go through before giving up */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          = (float *) malloc(sizeof(float)*Myrows);

= (float *) malloc(sizeof(float)*(Myrows*n_off_proc));

= (float *) malloc(sizeof(float)*(Myrows*n_off_proc));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             float *pcg(sr,n_off_proc,rhs,epsilon,max_iters, n_iter)
                                                                                                                                                                     /* return a*x[1] + y[1] (saxpy vector operation) */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           temp = (float *) malloc(sizeof(float)*Myrows);
z = (float *) malloc(sizeof(float)*Myrows);
r = (float *) malloc(sizeof(float)*Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       = (float *) malloc(sizeof(float) *Myrows);
                                                                     gssum(&result,1,&wrk); /* qlobal sum */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        result[1] = a*x[1]+y[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             /* choose initial guess */
result += x{1]*y[1];
                                                                                                                                                                                                                                                       vold saxpy(a,x,y,result,n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for ( 1=0; 1<Myrows; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for(1=0;1<n;1++)
                                                                                                                 return (result);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               float beta=0.0;
                                                                                                                                                                                                                                                                                                 float a;
float *x;
float *y;
float *result;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        old zTr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               new_zTr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        float alpha;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 float *temp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            float "p;
float "Kp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int *n_iter;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         float *z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     float 'x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              float *r;
                                                                                                                                                                                                                                                                                                                                                                                                                                            1nt 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int 1;
int );
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           float
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      float
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             float
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    float
                                                                                                                                                                                                                                                                                                                                                                                                int n;
```

```
for( ]=0; ]<Ncols[1]; ]++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1f ( index < Myrows )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1f ( index < Myrows )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for( 1=Myrows-1; 1>=0; 1-- )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /* - - - - - - - - +/
/* backward gauss-sledel +/
/* - - - - - - - - +/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for ( 1=0; 1<Myrows; 1++ )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         /* forward gauss-stedel
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   count --;
                                                                                                                                                                                                                                                                                                                                                                                                  for ( 1=0; 1<Myrows; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             count ++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sum = 0.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              /* for ( k=0; k<2; k++)
                                                                                                                                                     void precond( z, r)
                                                                                                                                                                                                                                                                                                                                                                                                                                         z[1] = 0.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    count = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   count--;
            *n_iter = 1;
return(x);
                                                                                                                                                                                                                                     int count,
                                                                                                                                                                                                                                                                              index,
                                                                                                                                                                                                                                                                                                                                                            float sum;
                                                                                                                                                                           float z[];
                                                                                                                                                                                               float r(];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        spmvm(sr,n_off_proc,p,Kp); /* K has already been stored don't worry */
                                                                                                                                                stored in each processor */
stored in each processor */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1f(mynode == 0) fprintf(stderr, "iteration alpha beta (r,r)\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             /* -- G quantity -- */
/* -- G quantity -- */
/* -- G quantity -- */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /* print out for checking intermediate results */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           beta = new_zTr / old_zTr; /* -- G quantity -- */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     -- G quantity
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               saxpy(alpha,p,x,x,Myrows); /* new x +/
saxpy(-alpha,Kp,r,r,Myrows); /* new r +/
                                                                                                                                   new_zTr = dot(z,r,Myrows); /* global dot
rTr = dot(r,r,Myrows); /* global dot
if( rTr < epsilon)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   saxpy(beta,p,z,p,Myrows); /* new p */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        1, alpha, beta, rTr, pKp);
                                                                                                                                                                                                                                                                                                                                                                                                     p[1] = z[1]; /* processor wise */
                                                                                                                                                                                                                                                                                                         /* - - - - - - - - - - - - - - - - //
/* Initialize the search direction */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      "td tf tf hf hr\n",
                                                                                                                                                                                                                                              return(x); /* processor wise */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 /* PCG loop in every processor */
                                                       old_zTr = new_zTr;
new_zTr = dot(z,r,Myrows);
rTr = dot(r,r,Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             saxpy (alpha, p, x, x, Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  pKp = dot (p, Kp, Myrows);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for( 1 =0; 1<max_lters; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     alpha = new_zTr / pKp;
                                                                                                                                                                                                                                                                                                                                                            for( 1=0; 1<Myrows; 1++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fprintf(stderr,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (rTr < epsilon)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1f( mynode()==0 )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               *n_iter = 1;
x[1] = 0;
 r[1] = rhs[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       brecond(z, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return(x);
                                                                                                                                                                                                                        *n iter = 0;
```

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elp2-new.c
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* preconditionig with the diagonal elements of the stiffness matrix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     sum -= z[index]*Vals[count];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sum -= z[index]*Vals[count];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        z[1] = (sum + r[1]) / Dlags[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      z[1] = (sum + r[1]) / Diags[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         index = LocalCols(count);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1ndex = LocalCols(count);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for( ]=0; ]<Ncols[1]; ]++ )
```